



Cambridge International AS & A Level

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NAME

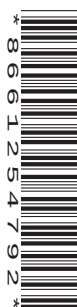


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FURTHER MATHEMATICS

9231/43

Paper 4 Further Probability & Statistics

May/June 2024

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **12** pages.



- 1 A college uses two assessments, X and Y , when interviewing applicants for research posts at the college. These assessments have been used for a large number of applicants this year.

The scores for a random sample of 9 applicants who took assessment X are as follows.

21.4 24.6 25.3 22.7 20.8 21.5 22.9 21.3 22.3

The scores for a random sample of 10 applicants who took assessment Y are as follows.

20.9 23.5 24.8 21.9 23.4 24.0 23.8 24.1 25.1 25.8

The interviewer believes that the population median score from assessment X is lower than the population median score from assessment Y .

Carry out a Wilcoxon rank-sum test, at the 1% significance level, to test whether the interviewer's belief is supported by the data. [7]

[illegible]

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3



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[illegible]



- 2 A rowing club has a large number of members. A random sample of 12 of these members is taken and the pulse rate, x beats per minute (bpm), of each is measured after a 30-minute training session. A 98% confidence interval for the population mean pulse rate, μ bpm, is calculated from the sample as $64.22 < \mu < 68.66$.

(a) Find the values of $\sum x$ and $\sum x^2$. [6]

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(b) State an assumption that is necessary for the confidence interval to be valid. [1]

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- 3 There are three bus companies in a city. The council is investigating whether the buses reliably arrive at their destination on time. The results from random samples of buses from each company are summarised in the following table.

		Bus company			Total
		<i>A</i>	<i>B</i>	<i>C</i>	
Arrival	Early	22	22	10	54
	On time	30	52	42	124
	Late	28	26	18	72
	Total	80	100	70	250

Test, at the 5% significance level, whether the reliability of buses is independent of bus company. [7]

[illegible]



4 The random variable X has probability generating function $G_X(t)$ given by

$$G_X(t) = ct(1+t)^5,$$

where c is a constant.

- (a) Find the value of c . [1]

- (b) Find the value of $E(X)$. [2]

[illegible]



The random variable Y is the sum of two independent values of X .

- (c) Write down the probability generating function of Y and hence find $\text{Var}(Y)$. [4]

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- (d)** Find $P(Y = 5)$. [2]

[illegible]



5 The continuous random variable X has cumulative distribution function F given by

$$F(x) = \begin{cases} 0 & x < 2, \\ \frac{(x-2)^2}{12} & 2 \leq x < 4, \\ 1 - \frac{(8-x)^2}{24} & 4 \leq x \leq 8, \\ 1 & x > 8. \end{cases}$$

(a) Sketch the graph of the probability density function of X .

[3]

(b) Find $E(X)$.

[3]

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(c) Find the exact value of the interquartile range of X .

[4]

[illegible]



Additional page

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